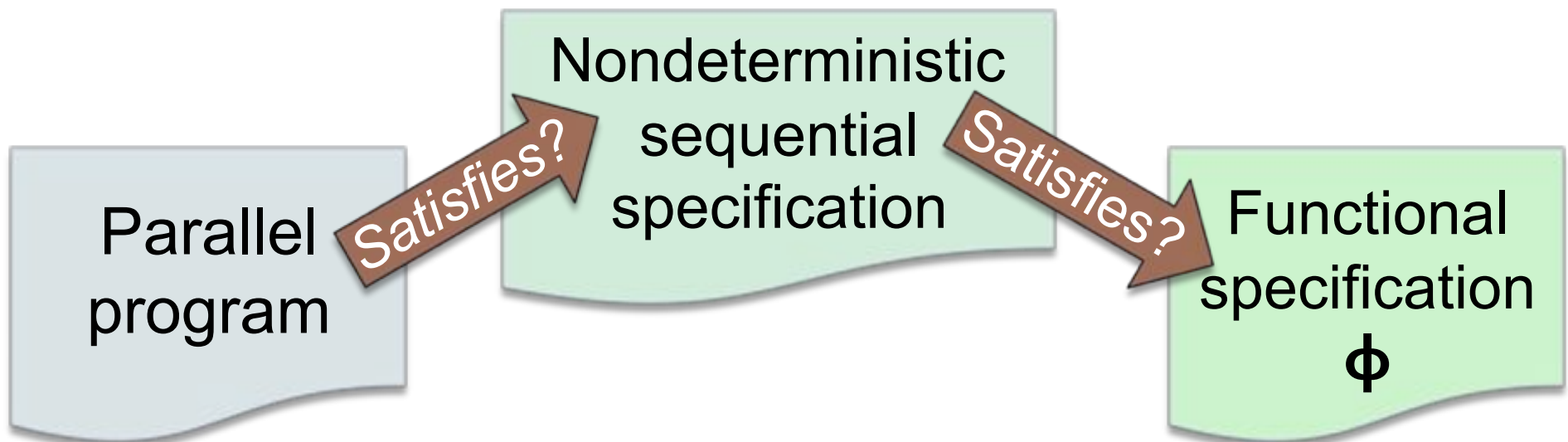


NDSeq: Runtime Checking for Nondeterministic Sequential Specs of Parallel Correctness

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Goal: Decompose effort in addressing parallelism and functional correctness



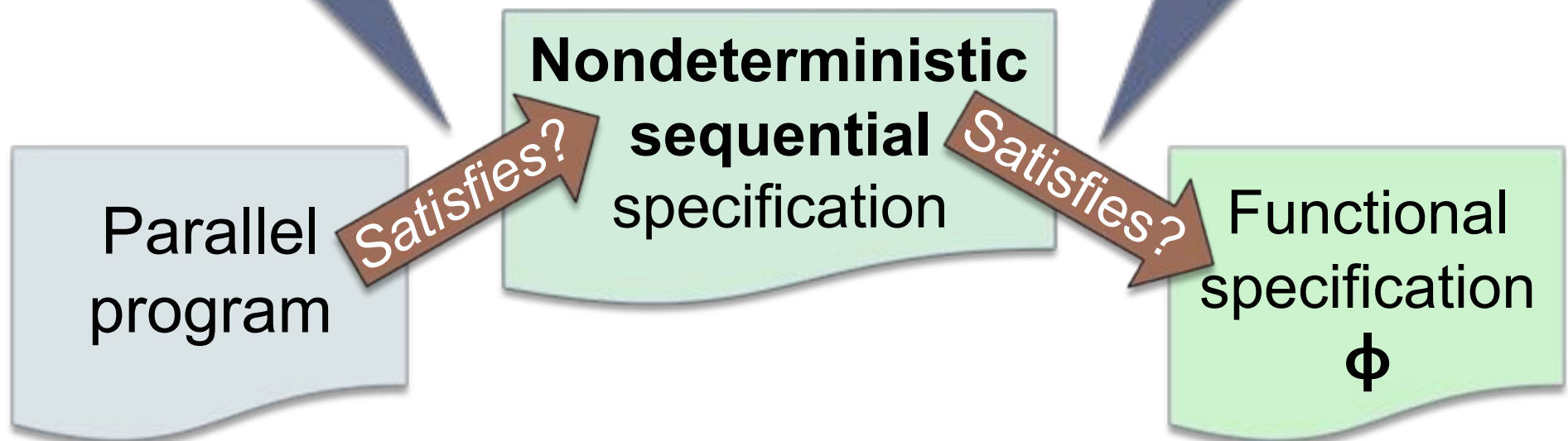
Goal: Decompose effort in addressing parallelism and functional correctness

Parallelism Correctness.

Handle independently of complex & sequential functional properties.

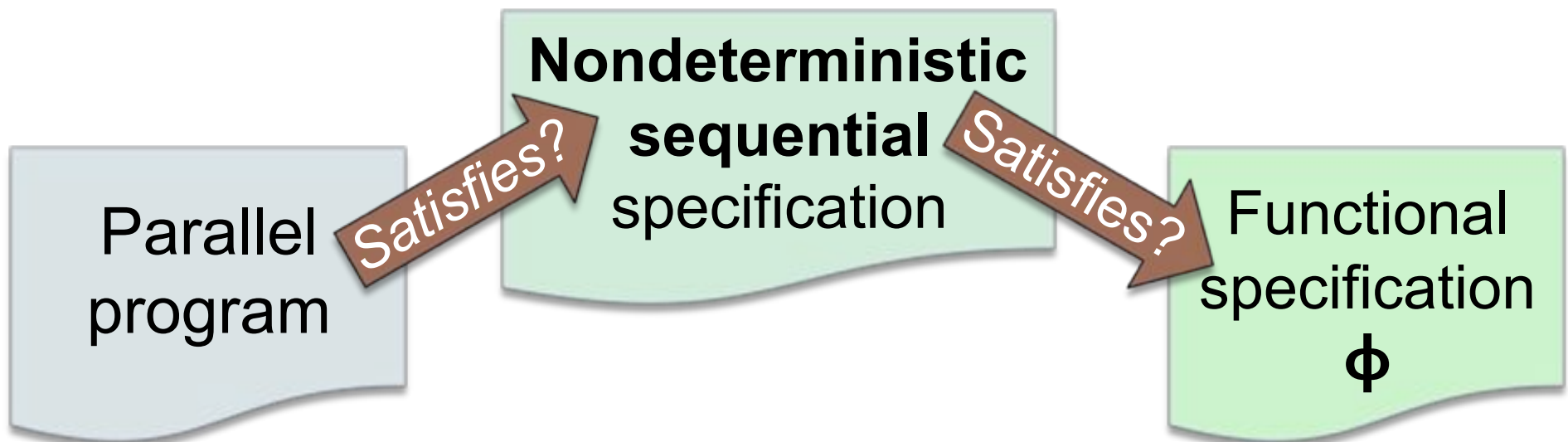
Functional Correctness.

Reason about sequentially, without thread interleavings.



Goal: Decompose effort in addressing parallelism and functional correctness

1. **NDSeq: easy-to-write spec for parallelism.**
2. **Runtime checking of NDSeq specifications.**



Outline

- ▶ Overview
- ▶ **Motivating Example**
- ▶ Nondeterministic Sequential (NDSeq) Specifications for Parallel Correctness
- ▶ Runtime Checking of NDSeq Specifications
- ▶ Experimental Results
- ▶ Conclusion

Motivating Example

- **Goal:** Find minimum-cost item in list.

```
for (i in [1..N]):  
    c = min_cost  
    b = lower_bound(i)  
    if b >= c:  
        continue  
    cost = compute_cost(i)  
    if cost < min_cost:  
        min_cost = cost  
        min_item = i
```

Input: N items.

Output: min_cost and min_item.

Motivating Example

- **Goal:** Find minimum-cost item in list.

```
for (i in [1..N]):  
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    continue  
  
  cost = compute_cost(i)  
  if cost < min_cost:  
    min_cost = cost  
    min_item = i
```

Computes **cheap** lower bound on cost of i.

Prune when i cannot have minimum-cost.

Computes cost of item i. **Expensive.**

Motivating Example

- **Goal:** Find minimum-cost item in list.

```
for (i in [1..N]):  
    c = min_cost  
    b = lower_bound(i)  
    if b >= c:  
        continue  
    cost = compute_cost(i)  
    if cost < min_cost:  
        min_cost = cost  
        min_item = i
```

How do we
parallelize this
code?

Parallel Motivating Example

- **Goal:** Find min-cost item in list, **in parallel**.

```
parallel-for (i in [1..N]):
```

```
  c = min_cost
```

```
  b = lower_bound(i)
```

```
  if b >= c:
```

```
    continue
```

```
  cost = compute_cost(i)
```

```
  synchronized (lock):
```

```
    if cost < min_cost:
```

```
      min_cost = cost
```

```
      min_item = i
```

Loop iterations can be run in **parallel**.

Updates to best are **protected by lock**.

Parallel Motivating Example

- **Goal:** Find min-cost item in list, **in parallel**.

```
parallel-for (i in [1..N]):  
  c = min_cost  
  b = lower_bound(i)  
  if b >= c:  
    continue  
  cost = compute_cost(i)  
  synchronized (lock):  
    if cost < min_cost:  
      min_cost = cost  
      min_item = i
```

Claim: Parallelization
is clearly correct.

How can we specify
this parallel
correctness?

Specifying Parallel Correctness

- **Idea:** Use sequential program as spec.

parallel-for (i in [1..N]):

c = min_cost

b = lower_bound(i)

if b >= c:

continue

cost = compute_cost(i)

synchronized (lock):

if cost < min_cost:

min_cost = cost

min_item = i

No.

Satisfies?

for (i in [1..N]):

c = min_cost

b = lower_bound(i)

if b >= c:

continue

cost = compute_cost(i)

if cost < min_cost:

min_cost = cost

min_item = i

Parallel-Sequential Equivalence?

items: (1) bound: 5
 cost: 5 (2) bound: 5
 cost: 5 min_item: –
 min_cost: ∞

parallel-for (i in [1..N]):

c = min_cost

b = lower_bound(i)

if b >= c:

continue

cost = compute_cost(i)

synchronized (lock):

if cost < min_cost:

min_cost = cost

min_item = i

prune?(1)



Parallel-Sequential Equivalence?

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parallel-for (i in [1..N]):

c = min_cost

b = lower_bound(i)

if b >= c:

continue

cost = compute_cost(i)

synchronized (lock):

if cost < min_cost:

min_cost = cost

min_item = i

prune?(1)

prune?(2)



Parallel-Sequential Equivalence?

items: (1) bound: 5
cost: 5 (2) bound: 5
cost: 5 min_item: (2)
min_cost: 5

parallel-for (i in [1..N]):

c = min_cost

b = lower_bound(i)

if b >= c:

continue

cost = compute_cost(i)

synchronized (lock):

if cost < min_cost:

min_cost = cost

min_item = i

prune?(1)

prune?(2)

update(2)



Parallel-Sequential Equivalence?

items: (1) bound: 5
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 min_cost: 5

parallel-for (i in [1..N]):

c = min_cost

b = lower_bound(i)

if b >= c:

continue

cost = compute_cost(i)

synchronized (lock):

if cost < min_cost:

min_cost = cost

min_item = i

prune?(1)

prune?(2)

update(2)

update(1)



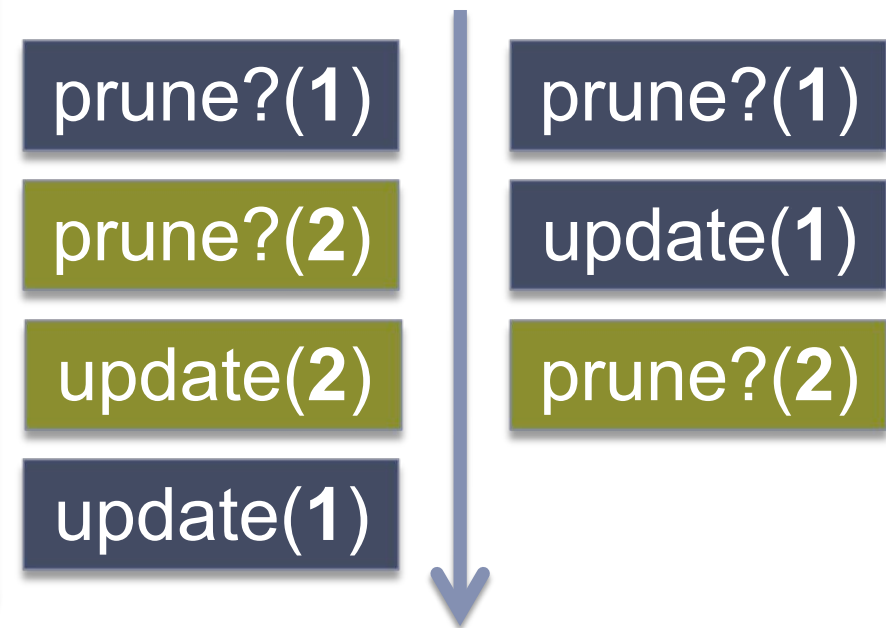
Parallel-Sequential Equivalence?

items: (1) bound: 5
 cost: 5 (2) bound: 5
 cost: 5 min_item: (2)
 min_cost: 5

```
parallel-for (i in [1..N]):  
  c = min_cost  
  b = lower_bound(i)  
  if b >= c:  
    continue  
  cost = compute_cost(i)  
  synchronized (lock):  
    if cost < min_cost:  
      min_cost = cost  
      min_item = i
```

But sequential program:

- Returns min_item = (1).
- Prunes (2).



Specifying Parallel Correctness

- ▶ Parallel program has freedom to:

```
parallel-for (i in [1..N]):  
  c = min_cost  
  b = lower_bound(i)  
  if b >= c:  
    continue  
  cost = compute_cost(i)  
  synchronized (lock):  
    if cost < min_cost:  
      min_cost = cost  
      min_item = i
```

Process items in a
nondeterministic order.

Avoid pruning by
scheduling check
before updates.

Specifying Parallel Correctness

Must give sequential spec this freedom.

```
parallel-for (i in [1..N]):  
  c = min_cost  
  b = lower_bound(i)  
  if b >= c:  
    continue  
  cost = compute_cost(i)  
  synchronized (lock):  
    if cost < min_cost:  
      min_cost = cost  
      min_item = i
```

Process items in a
nondeterministic order.

Avoid pruning by
scheduling check
before updates.

Nondeterministic Sequential Spec

Runs iterations **in any order**.

parallel-for (i in [1..N]):

c = min_cost

b = lower_bound(i)

if b >= c:

continue

Can **choose**
not to prune item.

min_cost = cost

min_item = i

nd-for (i in [1..N]):

c = min_cost

b = lower_bound(i)

if * && b >= c:

continue

cost = compute_cost(i)

if cost < min_cost:

min_cost = cost

min_item = i

NDSeq Specification Patterns

- ▶ Found three recipes for adding *'s:
 1. Optimistic Concurrent Computation
(optimistic work with conflict detection)
 2. Redundant Computation Optimization
(e.g., pruning in branch-and-bound)
 3. Irrelevant Computation
(e.g., updating a performance counter)
- ▶ With these recipes, fairly simple to write NDSeq specifications for our benchmarks.

Nondeterministic Sequential Spec

- ▶ Parallelism correct if no more nondeterminism:

parallel-for (i in [1..N]):

c = min_cost

b = lower_bound(i)

if b >= c:

continue

cost = compute_cost(i)

synchronized (lock):

if cost < min_cost:

min_cost = cost

min_item = i

Yes.

Satisfies?

nd-for (i in [1..N]):

c = min_cost

b = lower_bound(i)

if * && b >= c:

continue

cost = compute_cost(i)

if cost < min_cost:

min_cost = cost

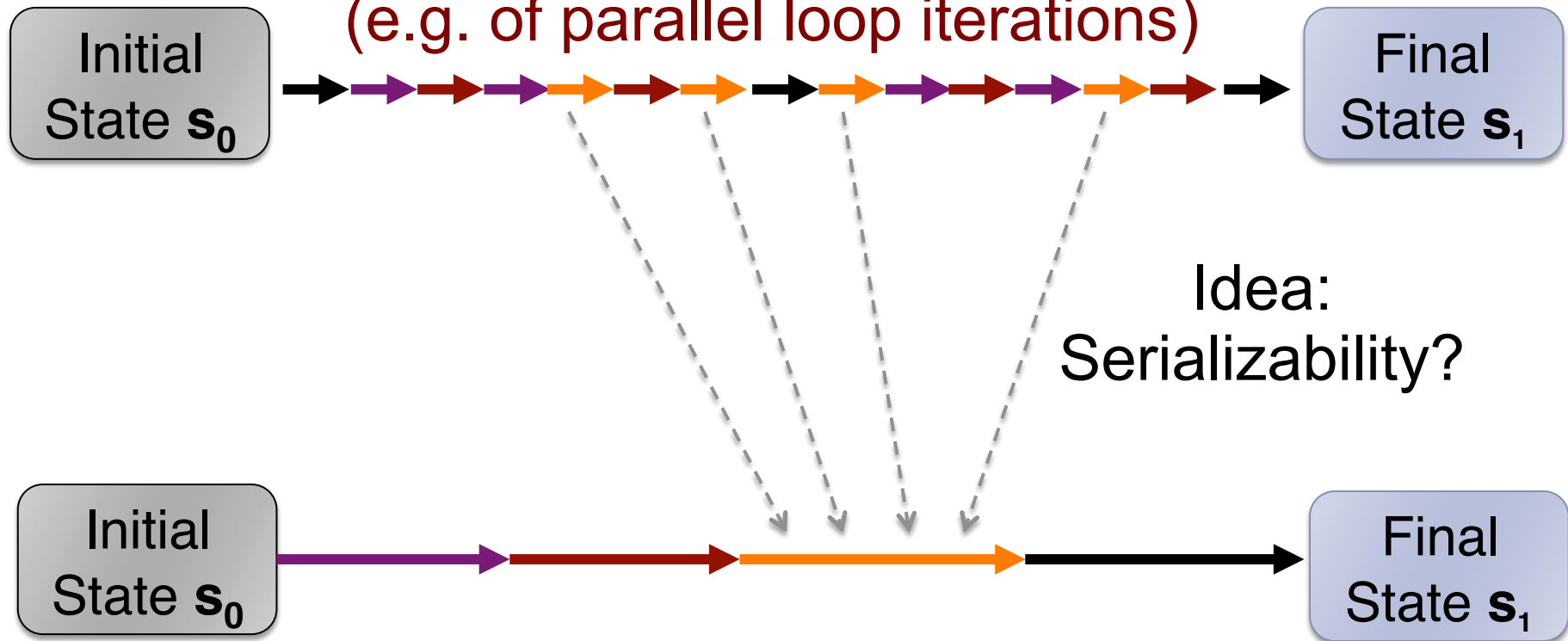
min_item = i

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Testing Parallelism Correctness

Given: an execution of parallel program
(e.g. of parallel loop iterations)



Is there an **equivalent** execution of NDSeq spec?

Conflict-Serializability is Too Strict

Thread 1:

```
c = min_cost
b = lower_bound(i)
if * [true]:
    if b >= c: // false

cost = compute_cost(i)
if cost < min_cost:
    // false
```

Classic Theorem:
Cycle of conflict edges =>
Not serializable!

Thread 2:

```
...
min_cost = cost
...
```


Relaxing Conflict-Serializability

Thread 1:

```
c = min_cost
b = lower_bound(i)
if * [true]:
    if b >= c: // false

cost = compute_cost(i)
if cost < min_cost:
    // false
```

Can we set * to false?

Check: Does body have any side effects on execution?

Thread 2:

```
...
min_cost = cost
...
```

Relaxing Conflict-Serializability

Thread 1:

```
c = min_cost
b = lower_bound(i)
if * [false]:
    if b >= c: // false

cost = compute_cost(i)
if cost < min_cost:
    // false
```

Can we set * to false?

Check: Does body have any side effects on execution?

Thread 2:

```
...
min_cost = cost
...
```

Relaxing Conflict-Serializability

Thread 1:

```
c = min_cost  
b = lower_bound(i)  
if * [false]:  
    if b >= c: // false  
  
cost = compute_cost(i)  
if cost < min_cost:  
    // false
```

Local **c** is no longer used,
so conflicting read of
min_cost is **irrelevant**.

Thread 2:

```
...  
min_cost = cost
```

Theorem. No **relevant**
conflict cycles => **exists**
equivalent NDSeq run!

Relaxing Conflict-Serializability

Theorem. No **relevant** conflict cycles => **exists equivalent NDSeq run!**

Iteration 1:

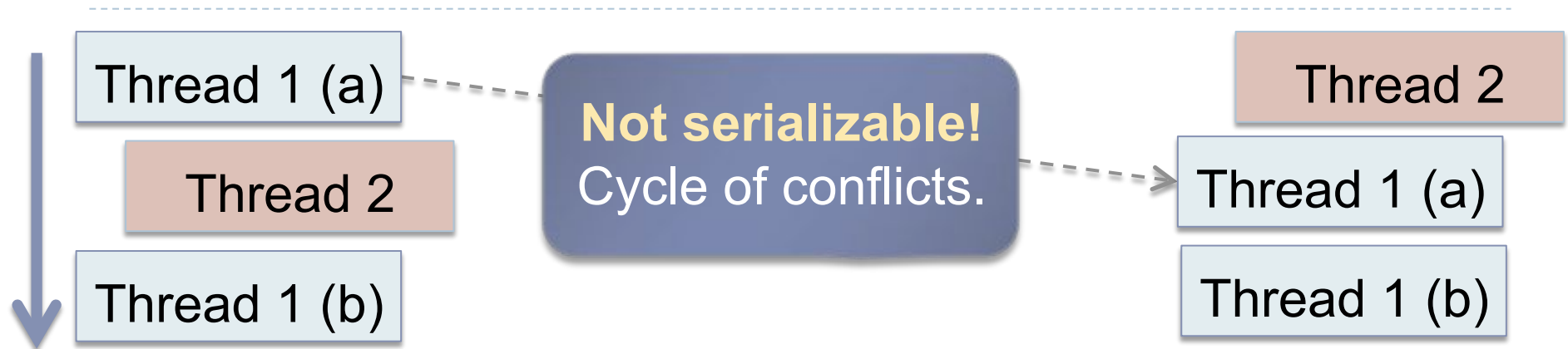
```
c = min_cost  
b = lower_bound(i)  
if * [false]:  
  
cost = compute_cost(i)  
if cost < min_cost:  
    // false
```

Iteration 2:

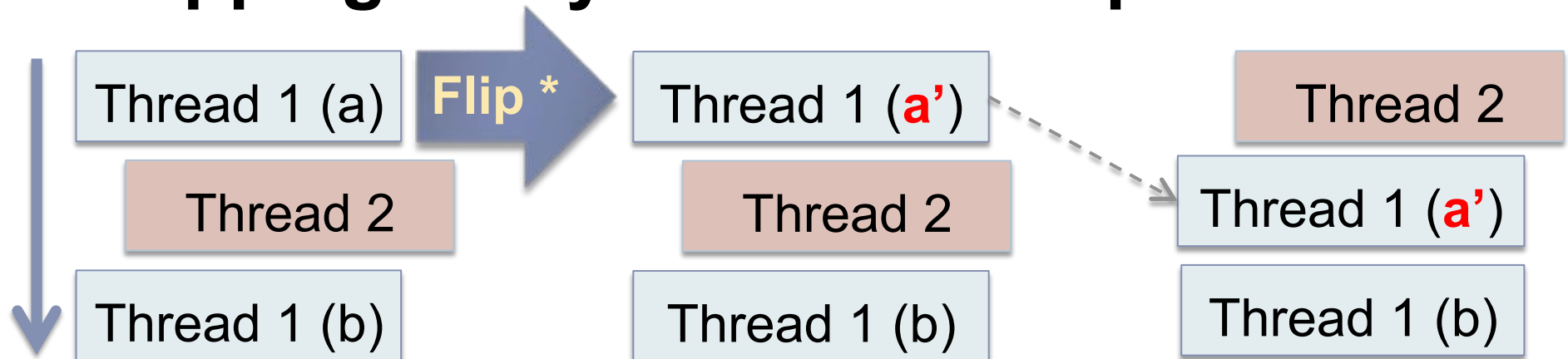
```
...  
min_cost = cost  
...
```

Read **different** value for min_cost, but **overall** behavior is the same.

Traditional conflict serializability:



+ flipping * + dynamic data dependence:



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Experimental Evaluation

- ▶ Wrote and tested NDSeq specifications for:
 - ▶ Java Grande, Parallel Java, Lonestar, DaCapo, and nonblocking data structure.
 - ▶ **Size:** 40 to 300K lines of code.
 - ▶ Tested 5 parallel executions / benchmark.
- ▶ **Two claims:**
 1. Easy to write NDSeq specifications.
 2. Our technique serializes significantly more executions than traditional methods.

Benchmark		Lines of Code	# of Parallel Constructs	# of if(*)
DaCapo	stack	40	1	2
	queue	60	1	2
	meshrefine	1K	1	2
	sunflow	24K	4	4
	xalan	302K	1	3
PJ	keysearch3	200	2	0
	mandelbrot	250	1	0
	phylogeny	4.4K	2	3
JGF	series	800	1	0
	crypt	1.1K	2	0
	raytracer	1.9K	1	0
	montecarlo	3.6K	1	0

Benchmark		Size of Trace	Serializability Warnings	
			Traditional	Our Technique
	stack	1,744	5 (false)	0
	queue	846	9 (false)	0
	meshrefine	747K	30 (false)	0
DaCapo	sunflow	24,250K	28 (false)	3 (false)
	xalan	16,540K	6 (false)	2 (false)
PJ	keysearch3	2,059K	2 (false)	0
	mandelbrot	1,707K	1 (false)	0
	phylogeny	470K	6	6
JGF	series	11K	0	0
	crypt	504K	0	0
	raytracer	6,170K	1	1
	montecarlo	1,897K	2 (false)	0

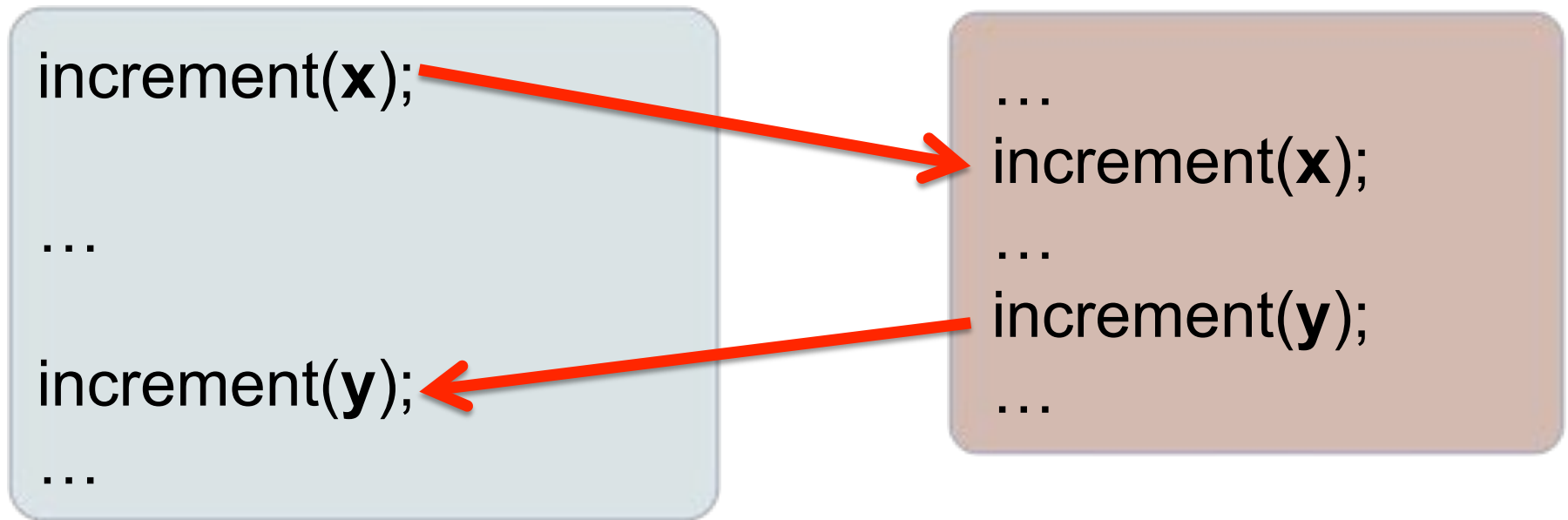
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JGF	series	11K	0	0
	crypt	504K	0	0
	raytracer	6,170K	1	1
	montecarlo	1,897K	2 (false)	0

Limitations

- ▶ Implementation

- ▶ Dynamic data dependence ==> high overhead.
- ▶ Instrumentation may miss some reads/writes.

- ▶ Commutativity:



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Summary

- ▶ **Separate parallel & functional correctness.**
 - ▶ Lightweight NDSeq specs for parallelism.
 - ▶ Sequentially verify functional correctness.
- ▶ **Runtime checking of NDSeq specs.**
 - ▶ Generalize conflict-serializability using $\text{if}(*)$ and dynamic data dependence.
- ▶ **Future/Current Work:**
 - ▶ Automatically inferring NDSeq specifications.
 - ▶ Static verification of parallel correctness.
 - ▶ Debugging on NDSeq.

Questions?

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and NSF for supporting this work.